

Collins' and Eisner's algorithms

Syntactic analysis/parsing

2017-12-07

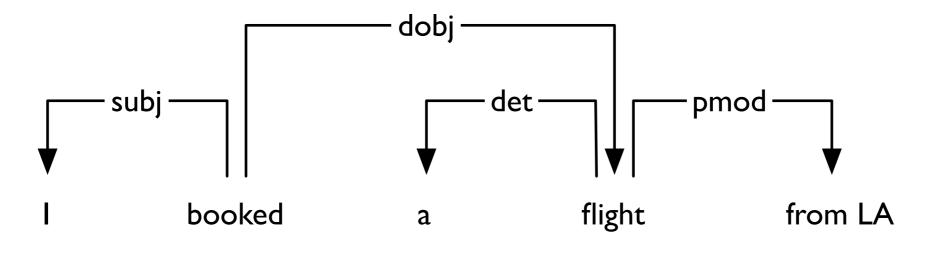
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Based on slides from Marco Kuhlmann

torsdag 7 december 17



Recap: Dependency trees



- In an arc $h \rightarrow d$, the word h is called the head, and the word d is called the dependent.
- The arcs form a rooted tree.



Recap: Scoring models and parsing algorithms

Distinguish two aspects:

- Scoring model: How do we want to score dependency trees?
 - Parsing algorithm:

How do we compute a highest-scoring dependency tree under the given scoring model?



Recap: The arc-factored model

- To score a dependency tree, score the individual arcs, and combine the score into a simple sum.
 score(t) = score(a₁) + ... + score(a_n)
- Define the score of an arc $h \rightarrow d$ as the weighted sum of all features of that arc:

$$score(h \rightarrow d) = f_1w_1 + \ldots + f_nw_n$$



Recap: Example features

- 'The head is a verb.'
- 'The dependent is a noun.'
- 'The head is a verb and the dependent is a noun.'
- 'The head is a verb and the predecessor of the head is a pronoun.'
- 'The arc goes from left to right.'
- 'The arc has length 2.'



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Arc-factored dependency parsing

Recap: Training using structured prediction

- Take a sentence *w* and a gold-standard dependency tree *g* for *w*.
- Compute the highest-scoring dependency tree under the current weights; call it p.
- Increase the weights of all features that are in g but not in p.
- Decrease the weights of all features that are in p but not in g.



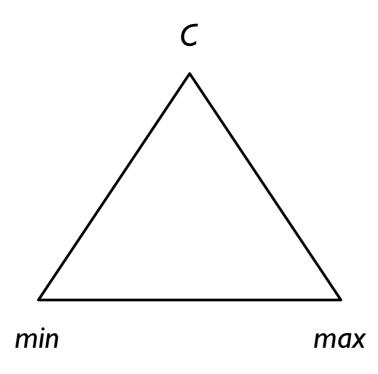
Recap: Collin's algorithm

- Collin's algorithm is a simple algorithm for computing the highest-scoring dependency tree under an arc-factored scoring model.
- It can be understood as an extension of the CKY algorithm to dependency parsing.
- Like the CKY algorithm, it can be characterized as a bottom-up algorithm based on dynamic programming.



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Recap: Signatures

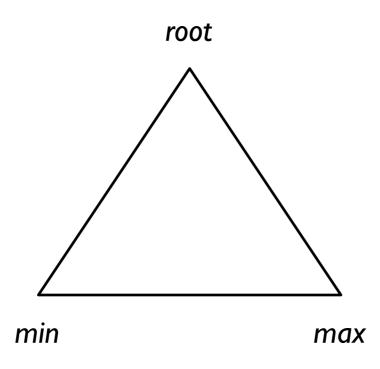


[min, max, C]



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Recap: Signatures

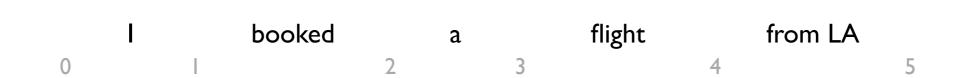


[min, max, root]



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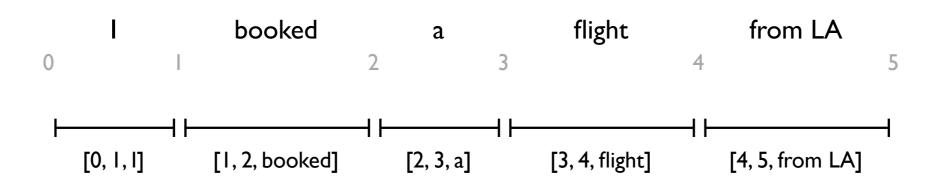
Recap: Initialization





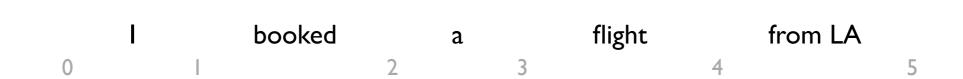
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Recap: Initialization



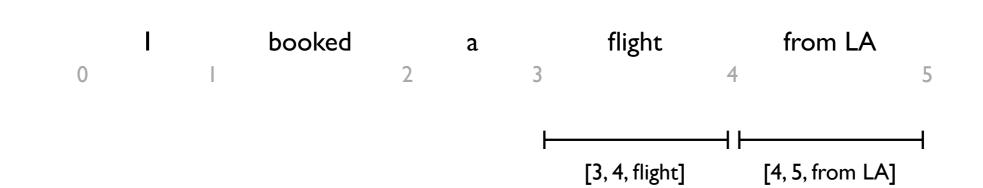


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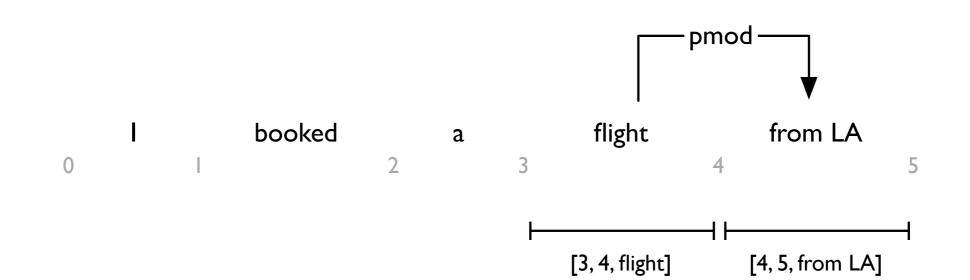


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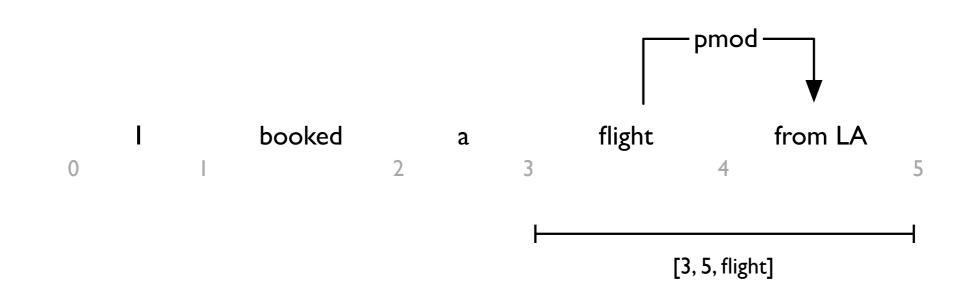


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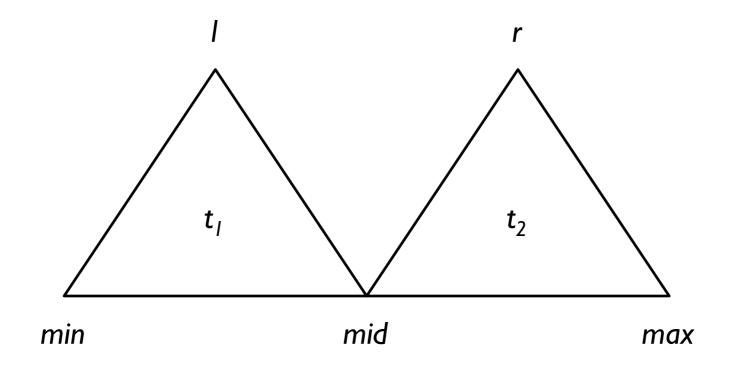




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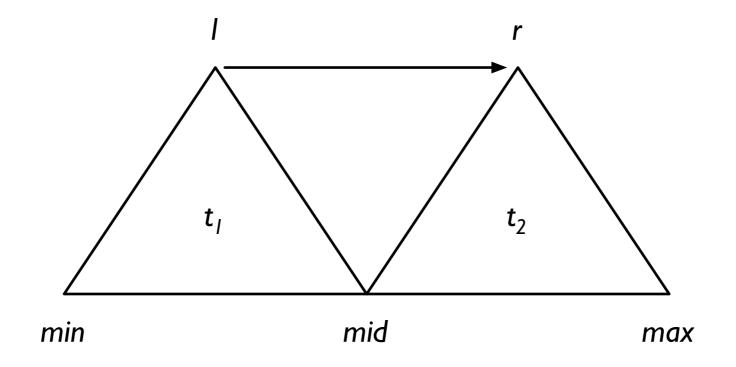


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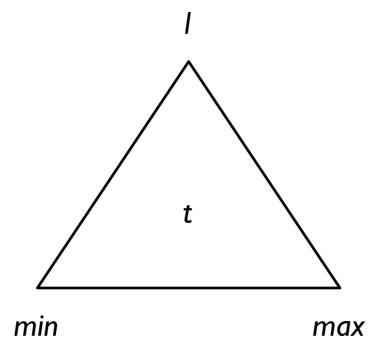


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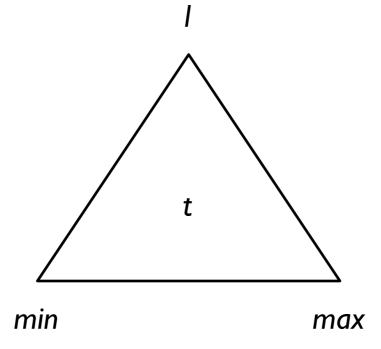


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$$score(t) = score(t_1) + score(t_2) + score(l \rightarrow r)$$





Adding a left-to-right arc

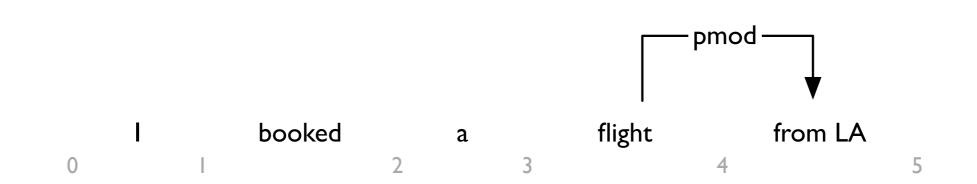
```
for each [min, max] with max - min > 1 do
  for each 1 from min to max - 2 do
    double best = score[min][max][1]
    for each r from 1 + 1 to max - 1 do
      for each mid from l + 1 to r do
        t<sub>1</sub> = score[min][mid][1]
         t<sub>2</sub> = score[mid][max][r]
         double current = t_1 + t_2 + score(1 \rightarrow r)
         if current > best then
           best = current
    score[min][max][1] = best
```



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Collins' algorithm





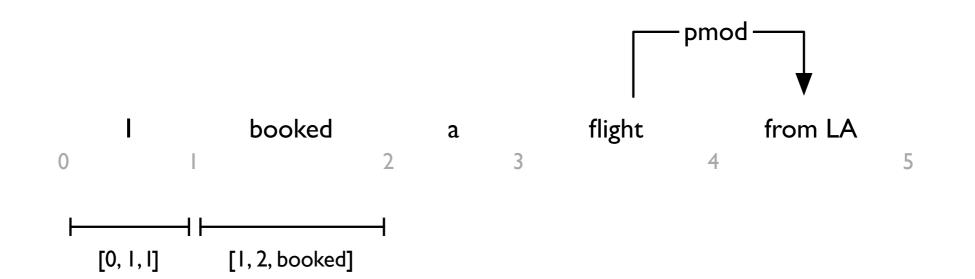


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Collins' algorithm

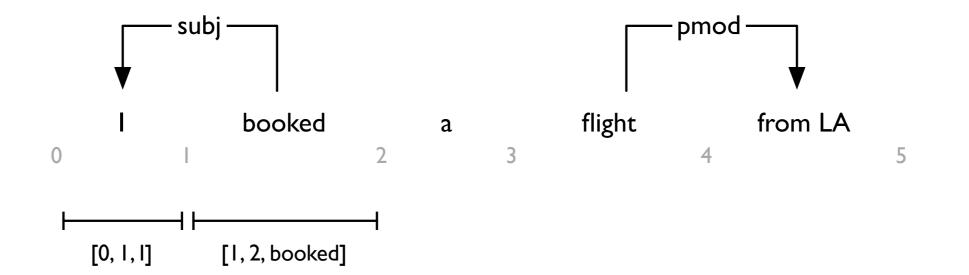








Adding a right-to-left arc



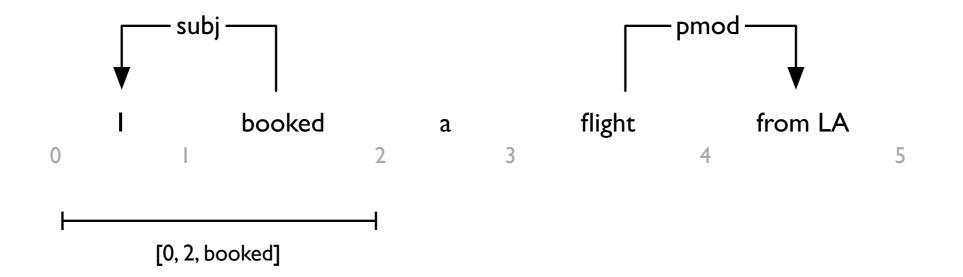


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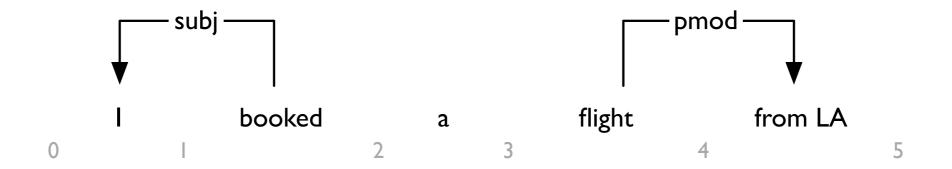
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Collins' algorithm

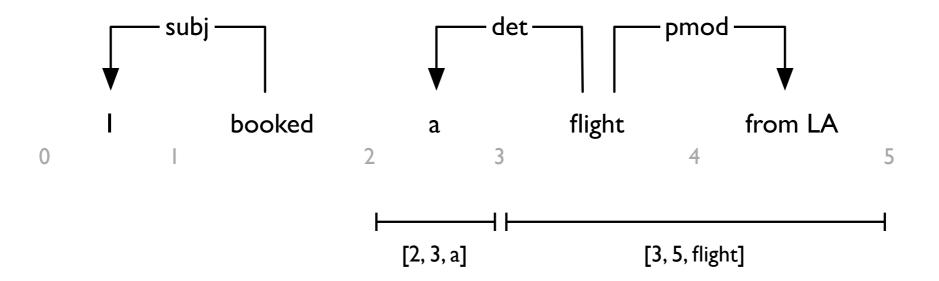




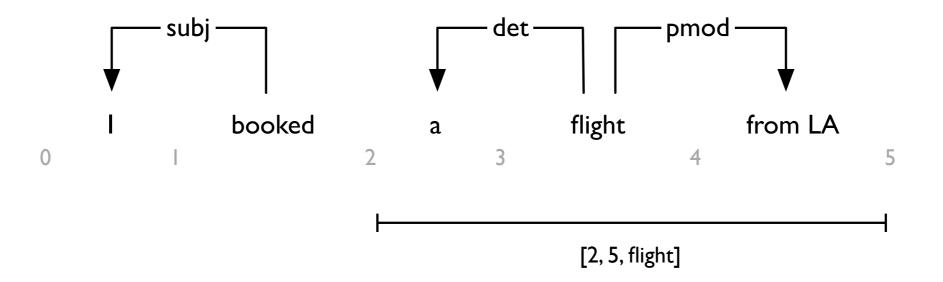




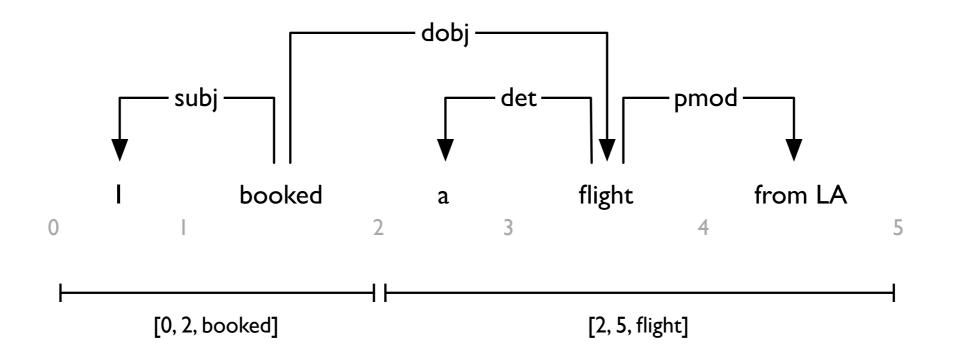








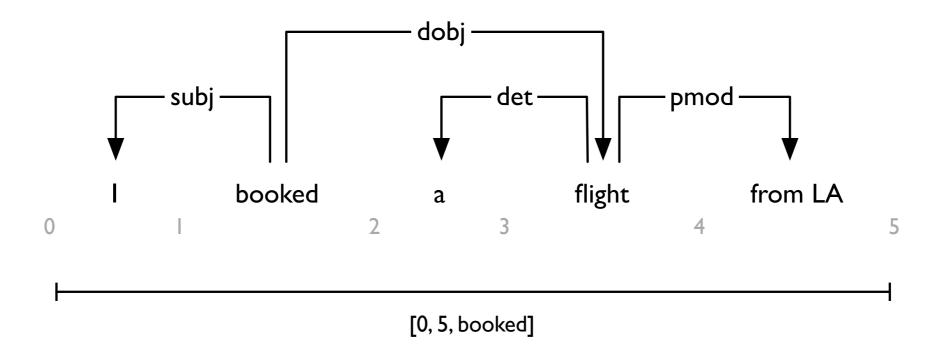






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Collins' algorithm





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Recap: Complexity analysis

- Space requirement: $O(|w|^3)$
- Runtime requirement: $O(|w|^5)$





Extension to the labeled case

- It is important to distinguish dependencies of different types between the same two words.
 Example: subj, dobj
- For this reason, practical systems typically deal with labeled arcs.
- The question then arises how to extend Collins' algorithm to the labeled case.



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Naive approach

- Add an innermost loop that iterates over all edge labels in order to find the combination that maximizes the overall score.
- For each step of the original algorithm, we now need to make |L| steps, where L is the set of all labels.





Smart approach

- Before parsing, compute a table that lists,
 for each head-dependent pair (h, d),
 the label that maximizes the score of arcs h → d.
- During parsing, simply look up the best label in the precomputed table.
- This adds (not multiplies!) a factor of $|L||w|^2$ to the overall runtime of the algorithm.



Summary

- Collins' algorithm is a CKY-style algorithm for computing the highest-scoring dependency tree under an arc-factored scoring model.
- It runs in time O(|w|⁵).
 This may not be practical for long sentences.



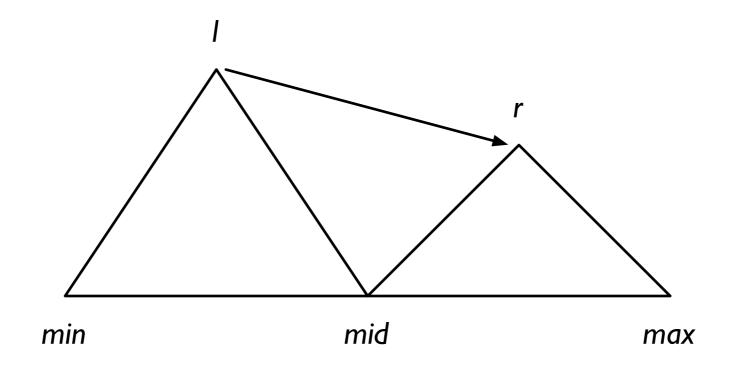
Eisner's algorithm



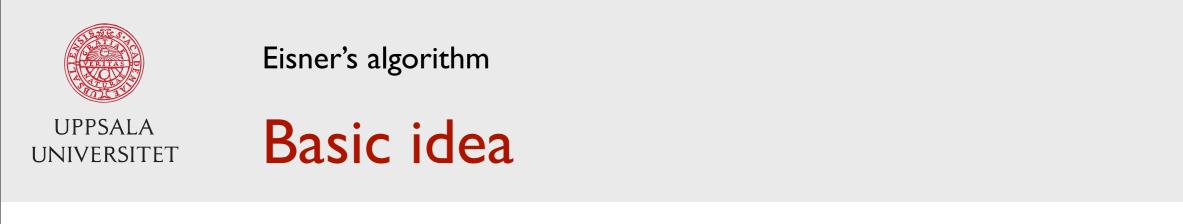
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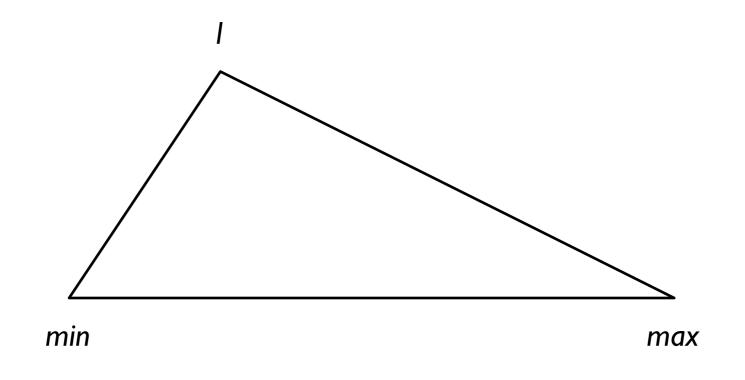
- With its runtime of $O(|w|^5)$, Collins' algorithm may not be of much use in practice.
- With Eisner's algorithm we will be able to solve the same problem in $O(|w|^3)$.
 - Intuition: collect left and right dependents independently





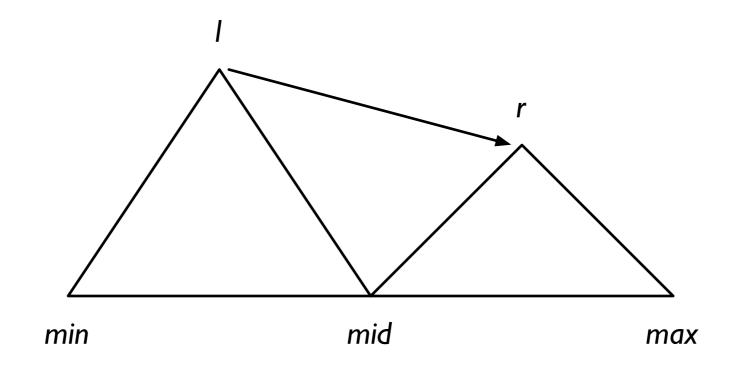
In Collins' algorithm, adding a left-to-right arc is done in one single step, specified by 5 positions.



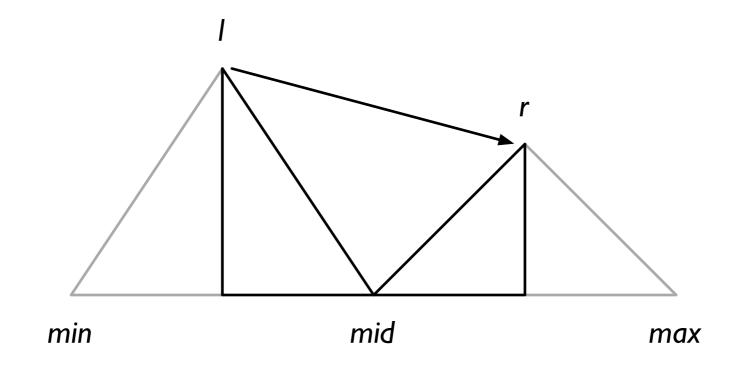


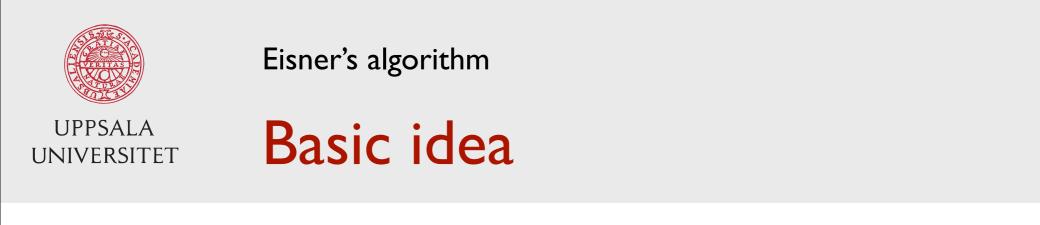
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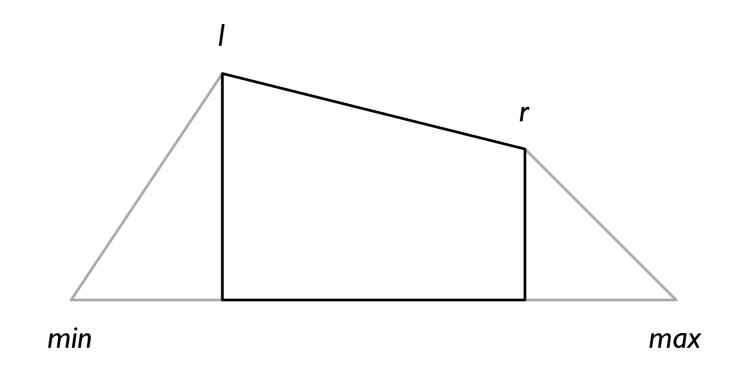


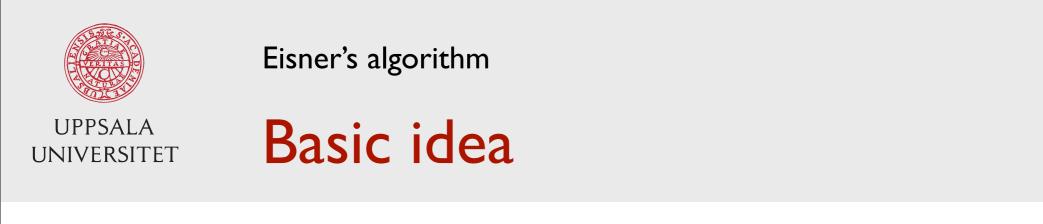


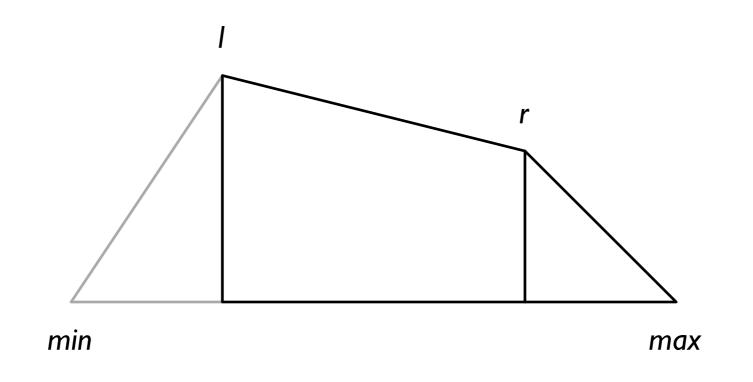




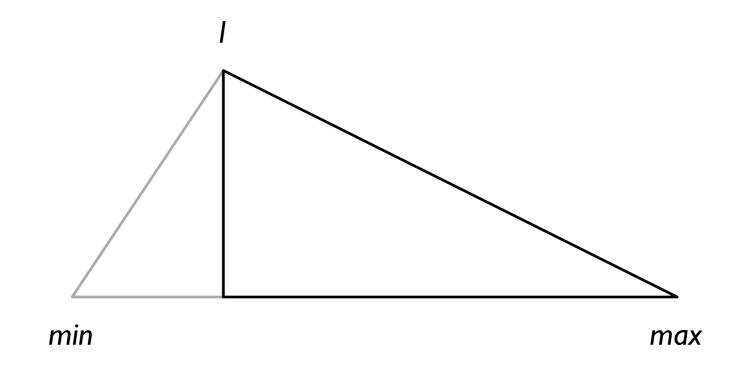




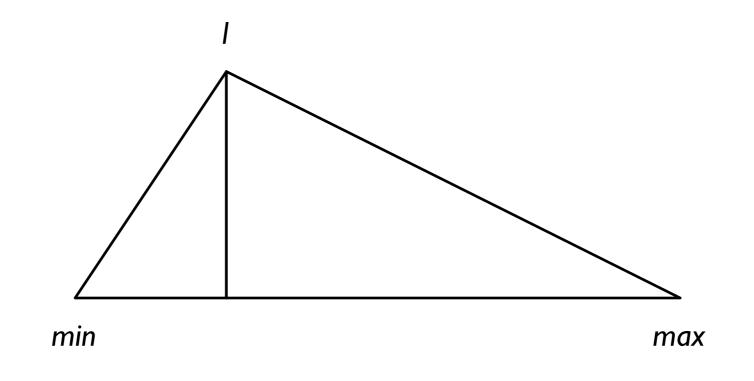


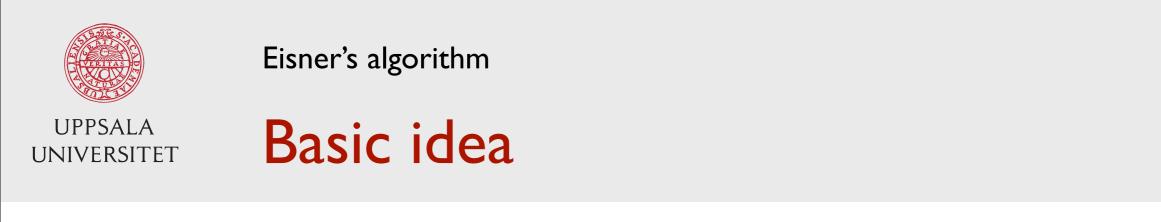


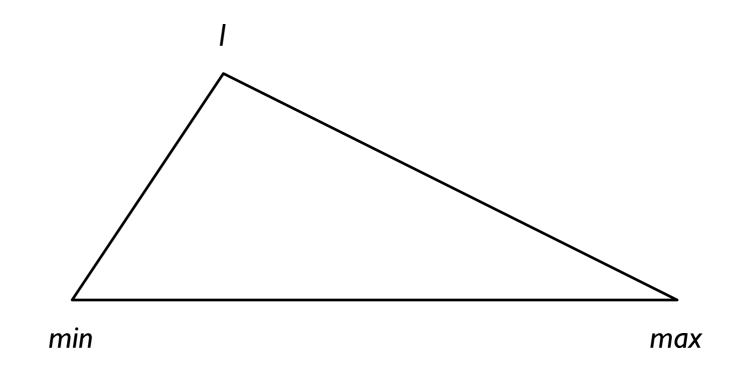






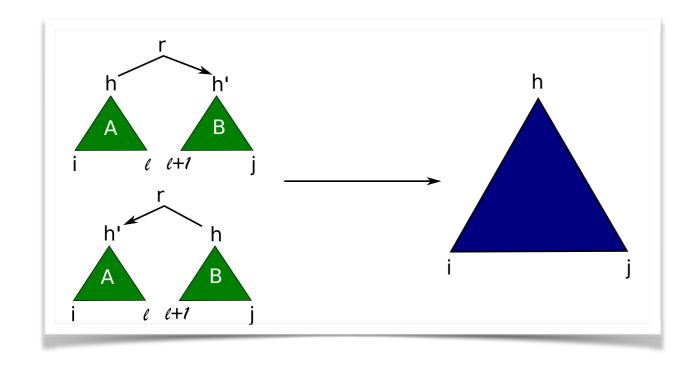


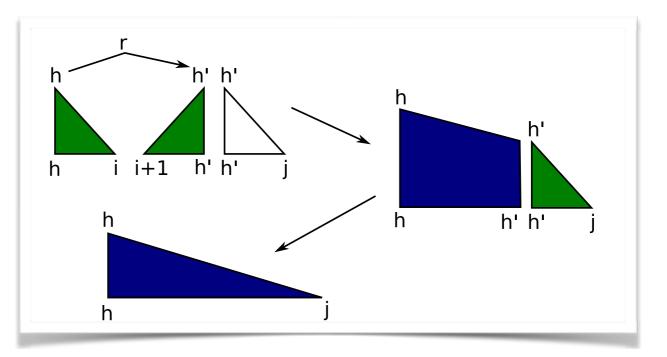






Eisner's algorithm





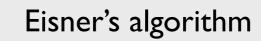


Eisner's algorithm

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Dynamic programming tables

- Collins':
 - [min,max,head]
- Eisner's
 - [min,max,head-side,complete]
 - head-side (binary): is head to the left or right?
 - complete (binary:) is the non-head side still looking for dependents?

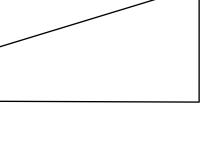




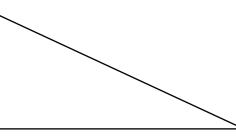
Graphic representation

• [min,max,left,yes]

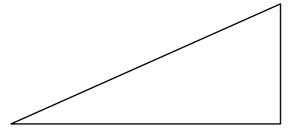
- [min,max,right,yes]



• [min,max,left,no]



• [min,max,right,no]

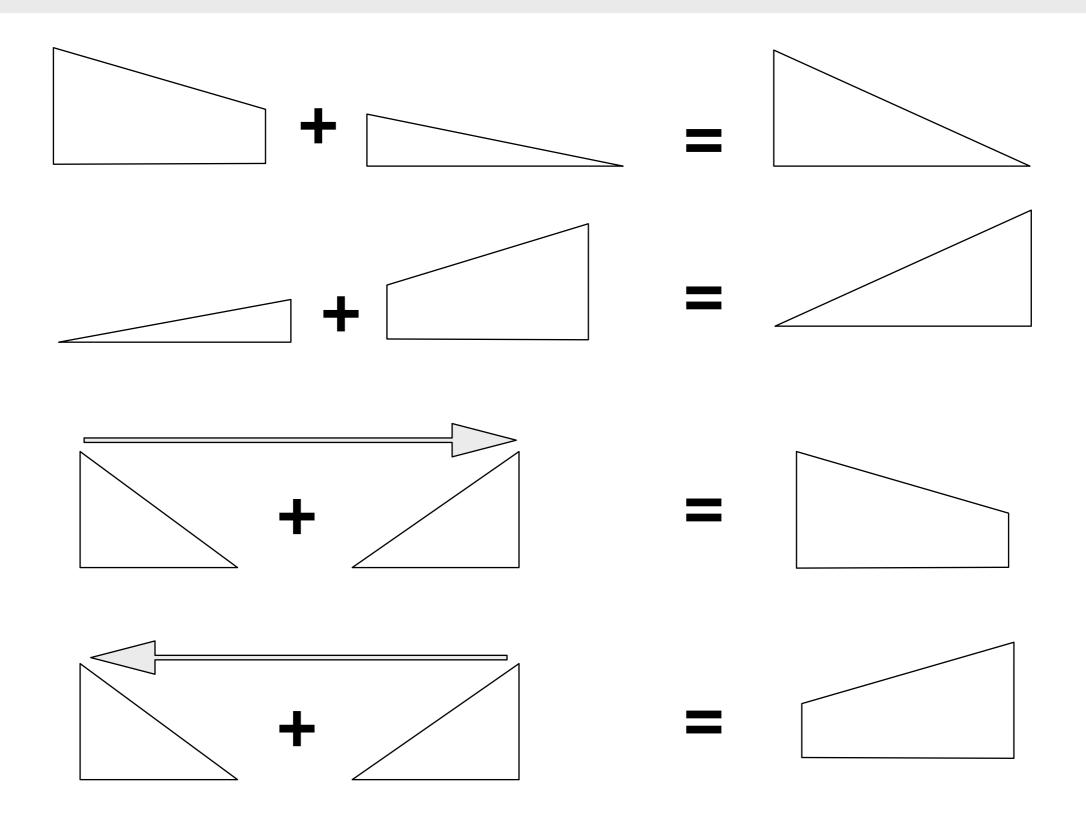




Eisner's algorithm

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Possible operations





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Eisner's algorithm

Pseudo code

```
for each i from 0 to n and all d,c do
   C[i][i][d][c] = 0.0
for each m from 1 to n do
   for each i from 0 to n-m do
       j = i+m
       C[i][j][\leftarrow][1] = \max_{i \le q < j}(C[i][q][\rightarrow][0] + C[q+1][j][\leftarrow][0] + score(w_j, w_i)
       C[i][j][\rightarrow][1] = \max_{i \leq q < j}(C[i][q][\rightarrow][0] + C[q+1][j][\leftarrow][0] + score(w_i, w_j)
       C[i][j][\leftarrow][0] = \max_{i \le q < j}(C[i][q][\leftarrow][0] + C[q][j][\leftarrow][1])
       C[i][j][\rightarrow][0] = \max_{i \le q \le j}(C[i][q][\rightarrow][1] + C[q][j][\rightarrow][0])
return [0][n][\rightarrow][0]
```



Summary

- Eisner's algorithm is an improvement over Collin's algorithm that runs in time $O(|w|^3)$.
- The same scoring model can be used.
- The same technique for extending the parser to labeled parsing can be used, adding O(|L||w|²) to the run time.
- Eisner's algorithm is the basis of current arc-factored dependency parsers.





Some animations

- Presentation by Terry Koo and Michael Collins:
 - <u>http://people.csail.mit.edu/maestro/papers/</u> <u>kool0acl-talk.pdf</u>
- Also contains a bit more information than this lecture.



Evaluation of dependency parsing



Evaluation of dependency parsers

- labelled attachment score (LAS): percentage of correct arcs, relative to the gold standard
- labelled exact match (LEM): percentage of correct dependency trees, relative to the gold standard
- unlabelled attachment score/exact match (UAS/ UEM):

the same, but ignoring arc labels



Word- vs sentence-level AS

- Example: 2 sentence corpus sentence 1: 9/10 arcs correct sentence 2: 15/45 arcs correct
- Word-level (*micro-average*):
 (9+15)/(10+45) = 24/55 = 0.436
- Sentence-level (macro-average):
 (9/10+15/45)/2 = (0.9+0.33)/2 = 0.617
- Word-level attachment score is normally used



Accuracy vs precision/recall

- Attachment score is an accuracy score
- For phrase-structure parsing we reported precision and recall
- Why is that not done for dependency parsing?



Own work

- Coming lectures: Dec 12, Dec 14
- Start looking at the dependency assignments! (all)
- Start looking at the seminar article (all)
- Do assignment 2, literature review (m)
- Decide on a project and start on it! (m 7.5)
- Plan your workload for your two courses early, and remember to plan for holidays as well!