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# The CKY algorithm part I: Recognition

Syntactic analysis (5LN455)

2016-11-10

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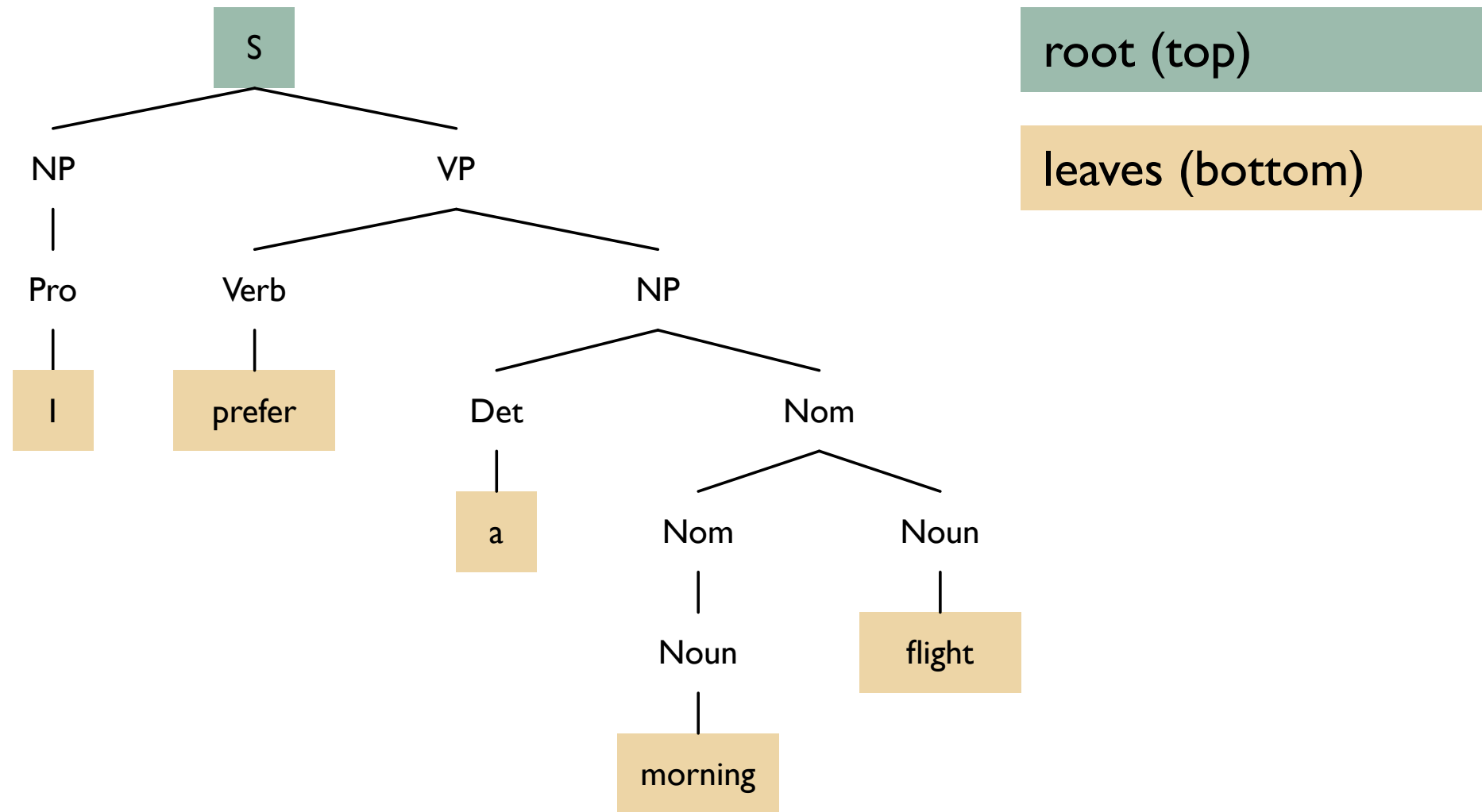
Department of Linguistics and Philology

Mostly based on slides from Marco Kuhlmann



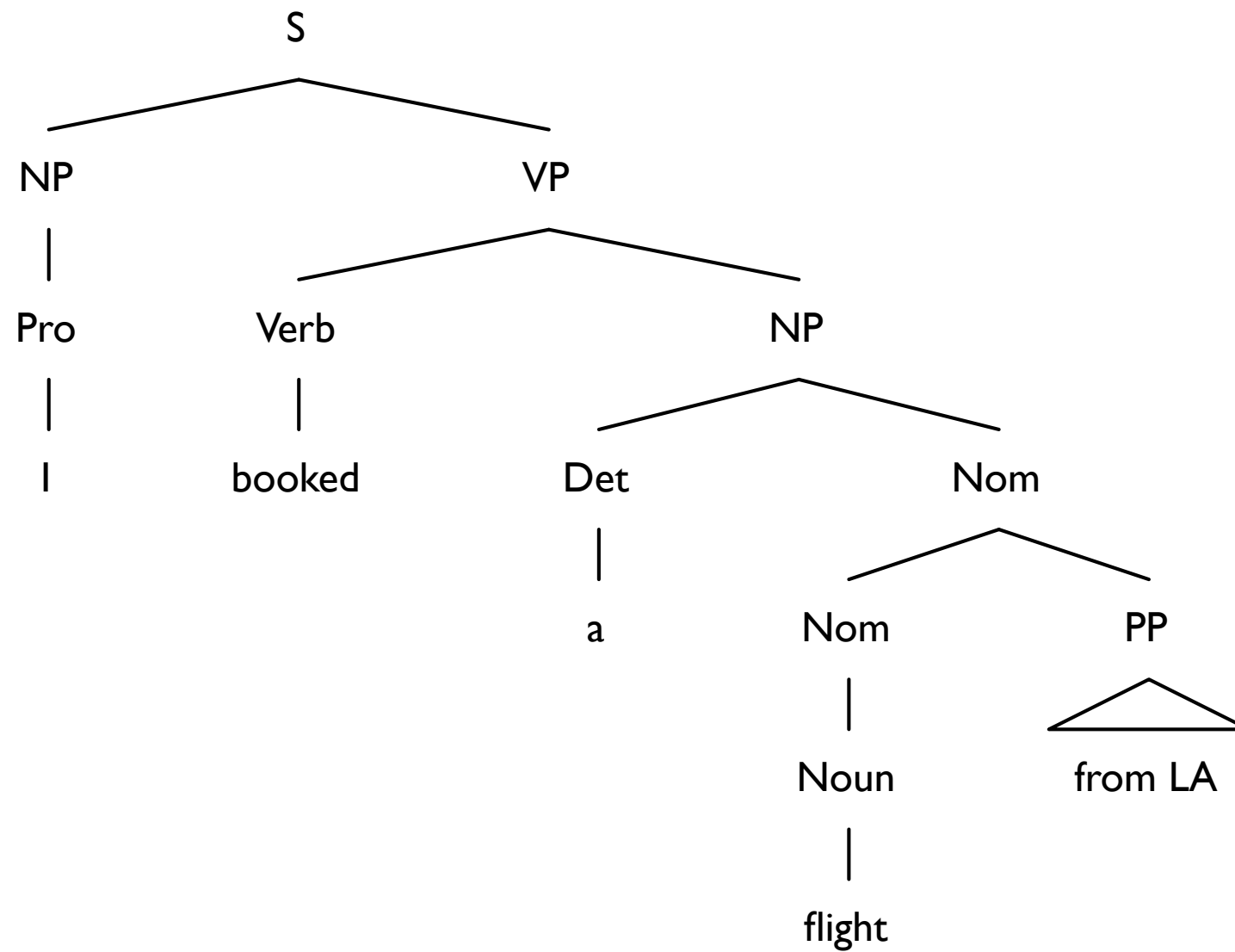


# Phrase structure trees



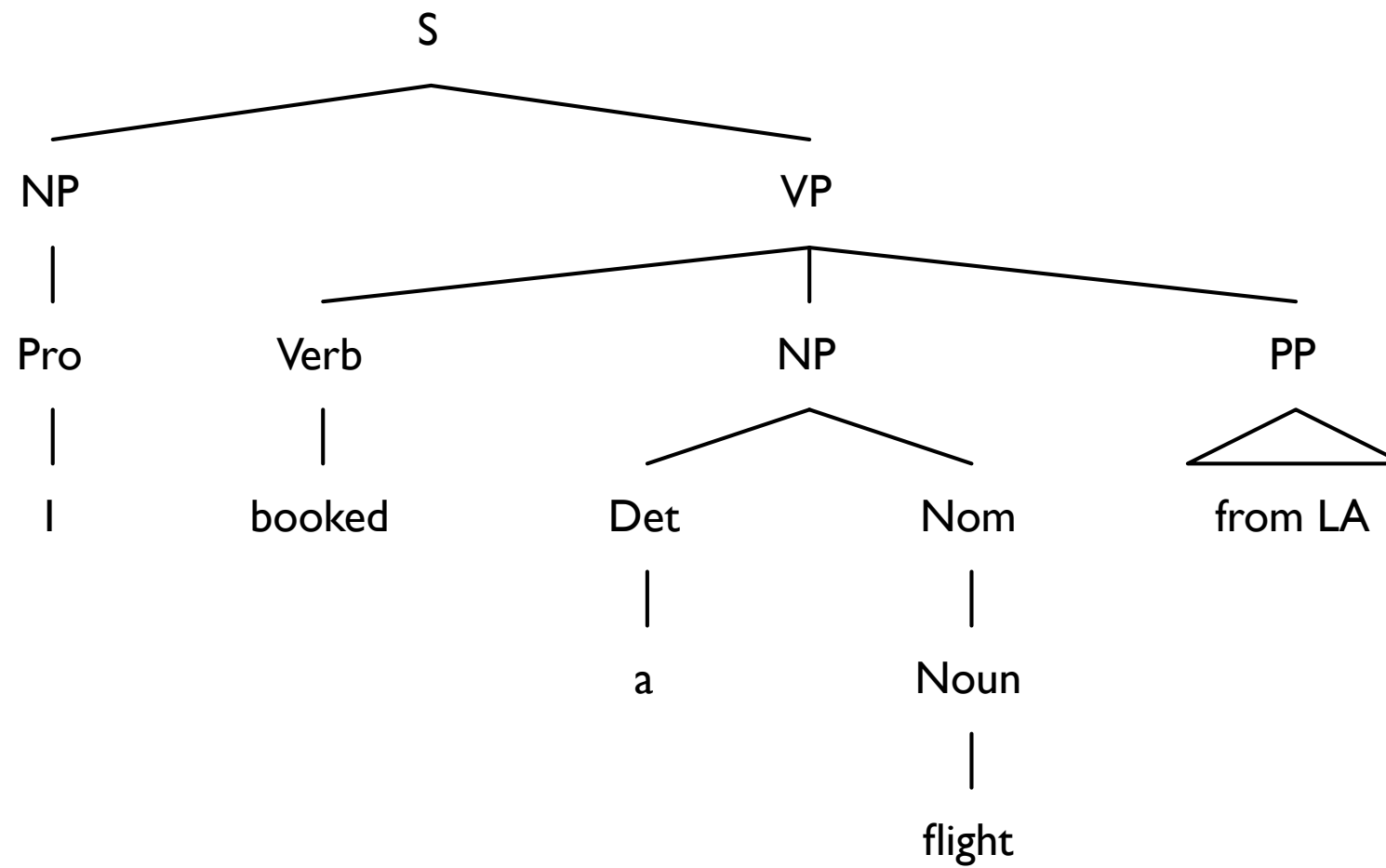


# Ambiguity





# Ambiguity





# Parsing as search

- **Parsing as search:**  
search through all possible parse trees  
for a given sentence
- **bottom–up:**  
build parse trees starting at the leaves
- **top–down:**  
build parse trees starting at the root node



# Overview of the CKY algorithm

- The CKY algorithm is an efficient bottom-up parsing algorithm for context-free grammars.
- It was discovered at least three (!) times and named after Cocke, Kasami, and Younger.
- It is one of the most important and most used parsing algorithms.



# Applications

The CKY algorithm can be used to compute many interesting things.

Here we use it to solve the following tasks:

- **Recognition:**  
Is there any parse tree at all?
- **Probabilistic parsing:**  
What is the most probable parse tree?



# Restrictions

- The original CKY algorithm can only handle rules that are at most binary:  
 $C \rightarrow w_i$  ,  $C \rightarrow C_1 C_2$  .
- It can easily be extended to also handle unit productions:  
 $C \rightarrow w_i$  ,  $C \rightarrow C_1$  ,  $C \rightarrow C_1 C_2$  .
- This restriction is not a problem theoretically, but requires preprocessing (binarization) and postprocessing (debinarization).
- A parsing algorithm that does away with this restriction is Earley's algorithm (Lecture 5 and J&M 13.4.2).





# Restrictions - details

- The CKY algorithm originally handles grammars in CNF (Chomsky normal form):  
 $C \rightarrow w_i, C \rightarrow C_1 C_2, (S \rightarrow \varepsilon)$
- $\varepsilon$  is normally not used in natural language grammars
- This is what you will use in assignment 2
- We will also discuss allowing unit productions,  $C \rightarrow C_1$ 
  - Extended CNF
  - Easy to integrate into CKY easier grammar conversions



# Conversion to CNF

- Eliminate mixed rules:
  - $VP \rightarrow V \text{ to } VP$  --  $VP \rightarrow V \text{ INF } VP$ ,  $\text{INF} \rightarrow \text{to}$
- Eliminate n-ary branching subtrees, with  $n > 2$ , by inserting additional nodes
  - $VP \rightarrow V \text{ INF } VP$  --  $VP \rightarrow V \text{ XI}$ ,  $\text{XI} \rightarrow \text{INF } V$
- Eliminate unary branching by merging nodes
  - $S \rightarrow \text{NP } VP$ ,  $\text{NP} \rightarrow \text{PRON}$ ,  $\text{PRON} \rightarrow \text{you}$  --  $\text{NP} \rightarrow \text{you}$



# Conversion to CNF

- Eliminate mixed rules:
  - $VP \rightarrow V \text{ to } VP$  --  $VP \rightarrow V \text{ INF } VP$ ,  $\text{INF} \rightarrow \text{to}$
- Eliminate n-ary branching subtrees, with  $n > 2$ , by inserting additional nodes
  - $VP \rightarrow V \text{ INF } VP$  --  $VP \rightarrow V \text{ XI}$ ,  $\text{XI} \rightarrow \text{INF } V$   
with markovization  $VP \rightarrow V \text{ VP} | V$ ,  $\text{VP} | V \rightarrow \text{INF } VP$
- Eliminate unary branching by merging nodes
  - $S \rightarrow \text{NP } VP$ ,  $\text{NP} \rightarrow \text{PRON}$ ,  $\text{PRON} \rightarrow \text{you}$  --  $\text{NP} \rightarrow \text{you}$   
with markovization  $\text{NP} \rightarrow \text{NP} + \text{PRON } VP$ ,  $\text{NP} + \text{PRON} \rightarrow \text{you}$



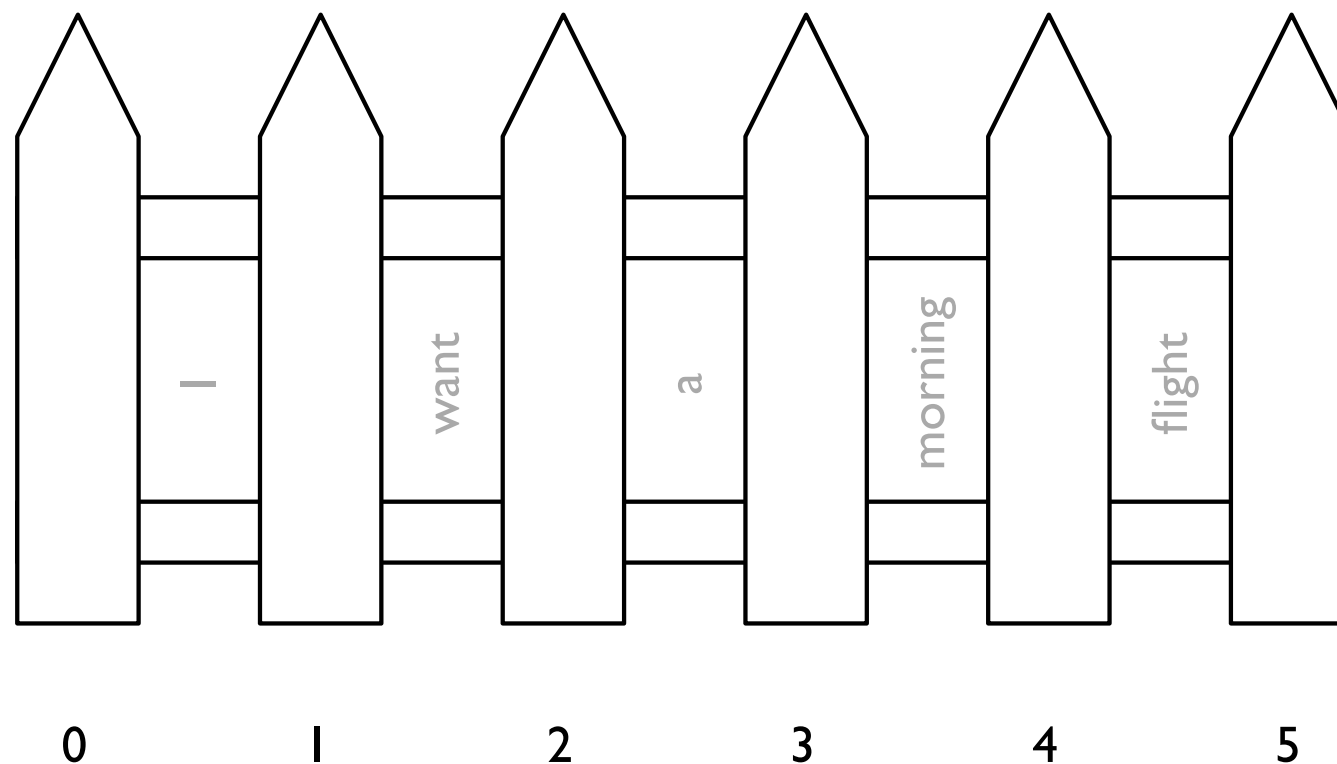
# Conventions

- We are given a context-free grammar  $G$  and a sequence of word tokens  $w = w_1 \dots w_n$ .
- We want to compute parse trees of  $w$  according to the rules of  $G$ .
- We write  $S$  for the start symbol of  $G$ .



# Fencepost positions

We view the sequence  $w$  as a fence with  $n$  holes,  
one hole for each token  $w_i$ ,  
and we number the fenceposts from 0 till  $n$ .





# Structure

- Is there any parse tree at all?
- What is the most probable parse tree?



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# Recognition



# Recognizer

A computer program that can answer the question

Is there any parse tree at all

for the sequence  $w$  according to the grammar  $G$ ?

is called a **recognizer**.

In practical applications one also wants

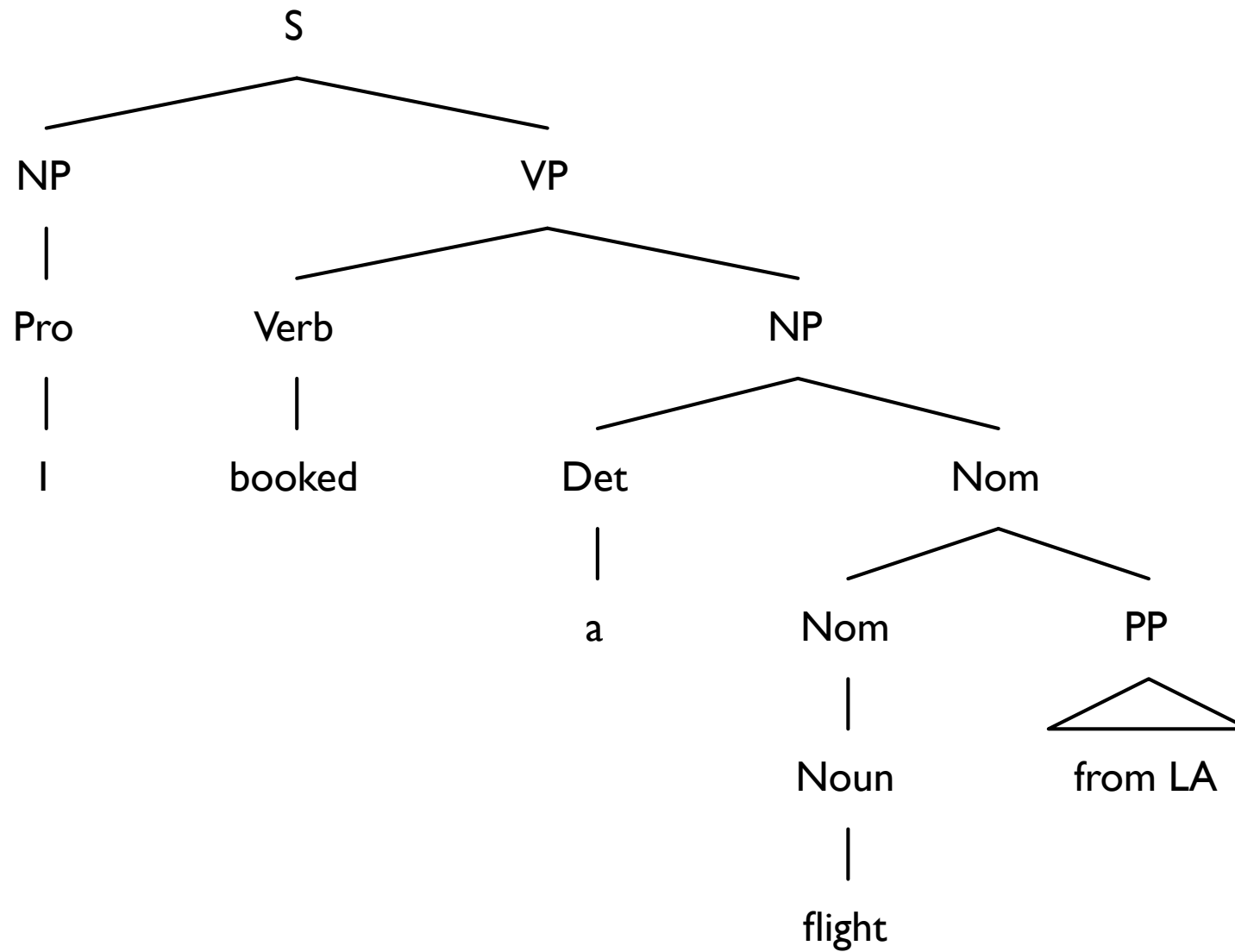
a concrete parse tree, not only an answer

to the question whether such a parse tree exists.





# Parse trees





# Preterminal rules and inner rules

- **preterminal rules:**

rules that rewrite a part-of-speech tag to a token, i.e. rules of the form  $C \rightarrow w_i$

Pro  $\rightarrow$  I, Verb  $\rightarrow$  booked, Noun  $\rightarrow$  flight

- **inner rules:**

rules that rewrite a syntactic category to other categories:  $C \rightarrow C_1 C_2$ ,  $(C \rightarrow C_1)$

S  $\rightarrow$  NP VP, NP  $\rightarrow$  Det Nom, (NP  $\rightarrow$  Pro)



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Recognition

# Recognizing small trees

$w_i$



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# Recognizing small trees

$$C \rightarrow w_i$$

$w_i$



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Recognition

# Recognizing small trees

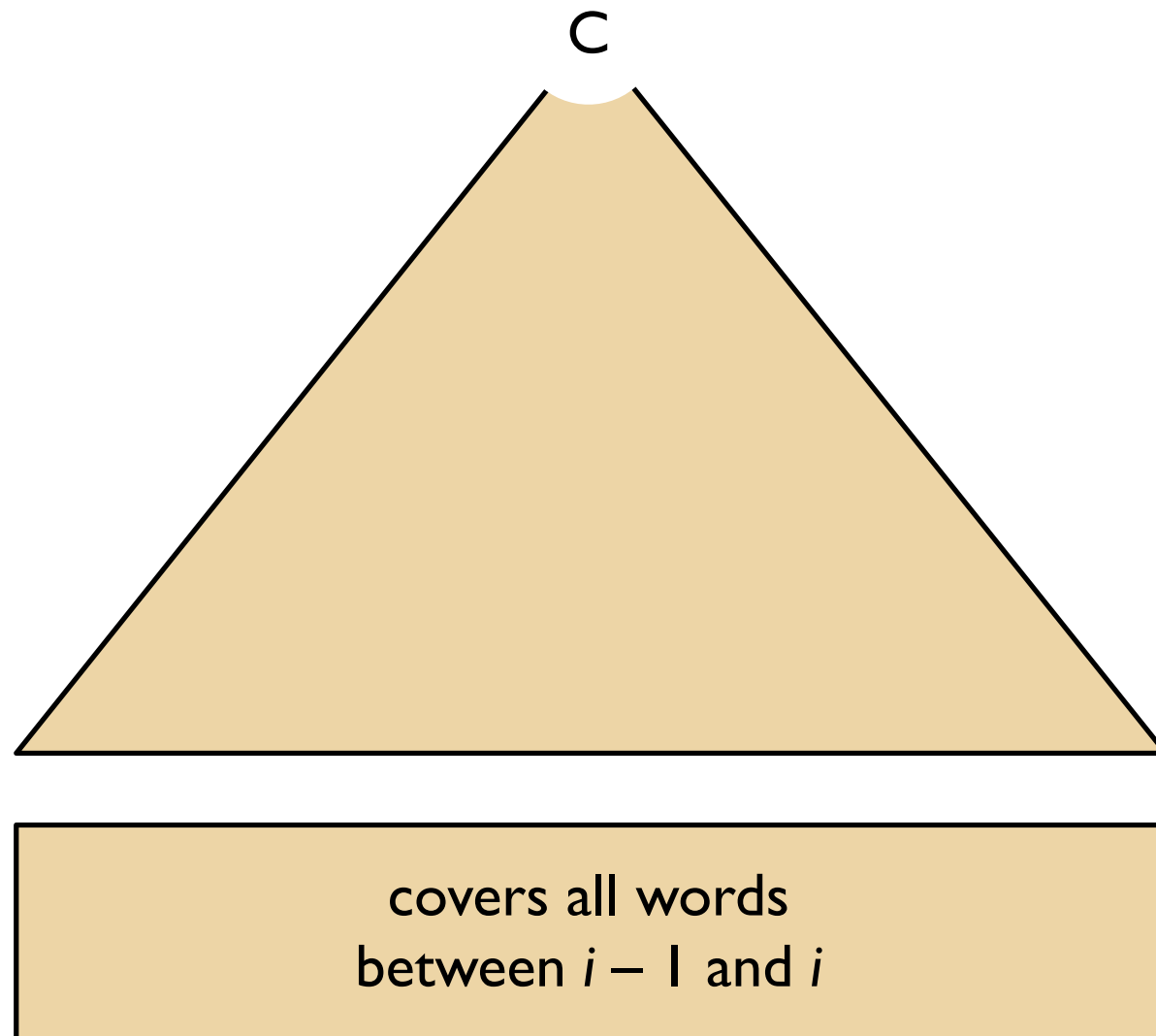




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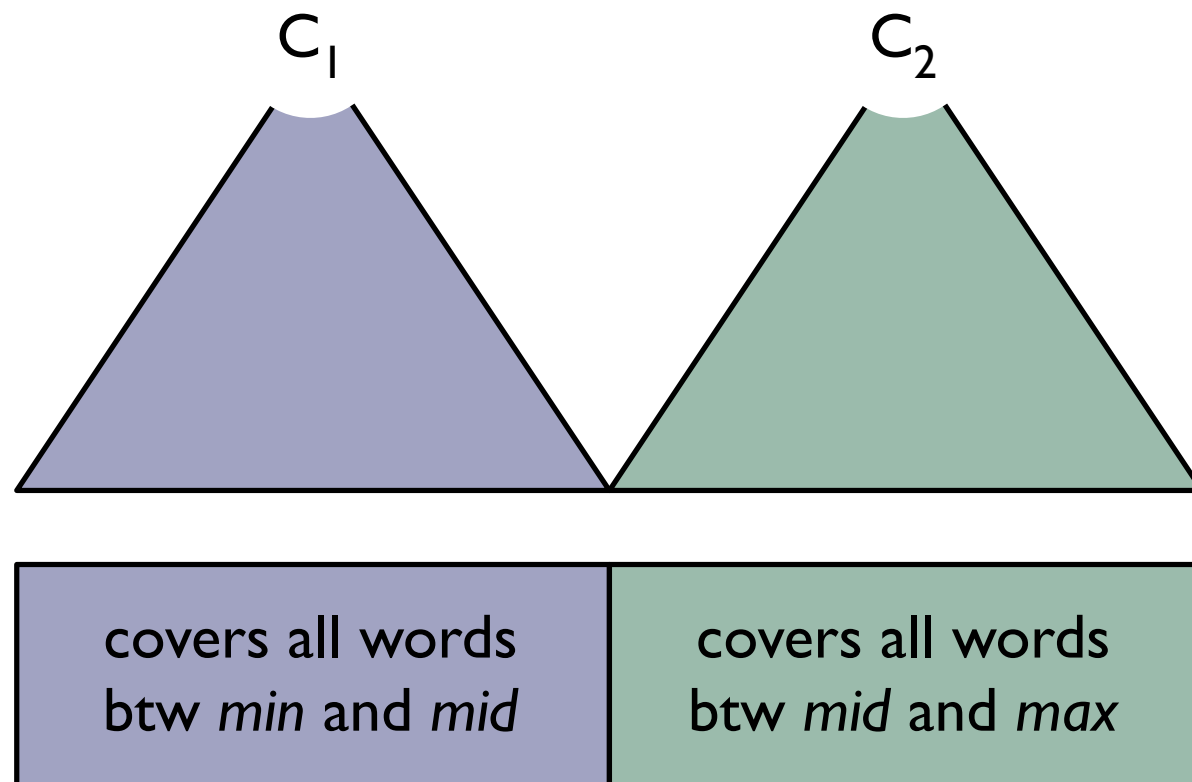
Recognition

# Recognizing small trees





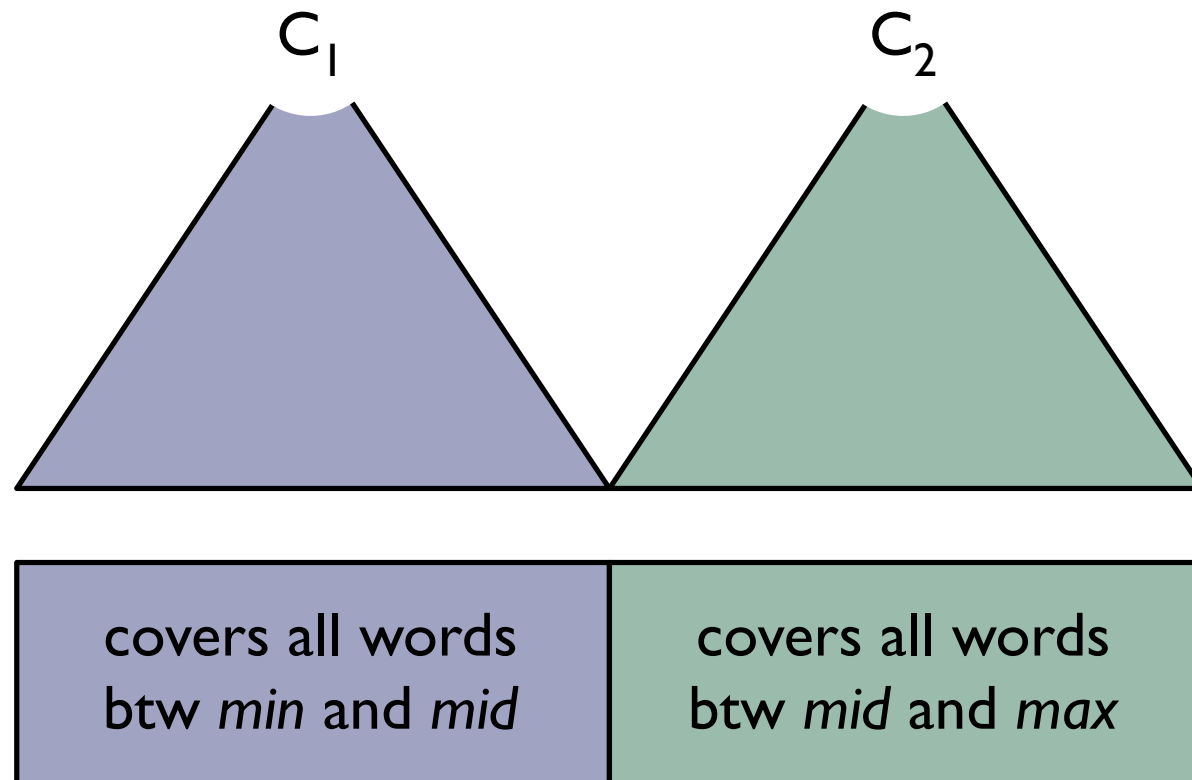
# Recognizing big trees





# Recognizing big trees

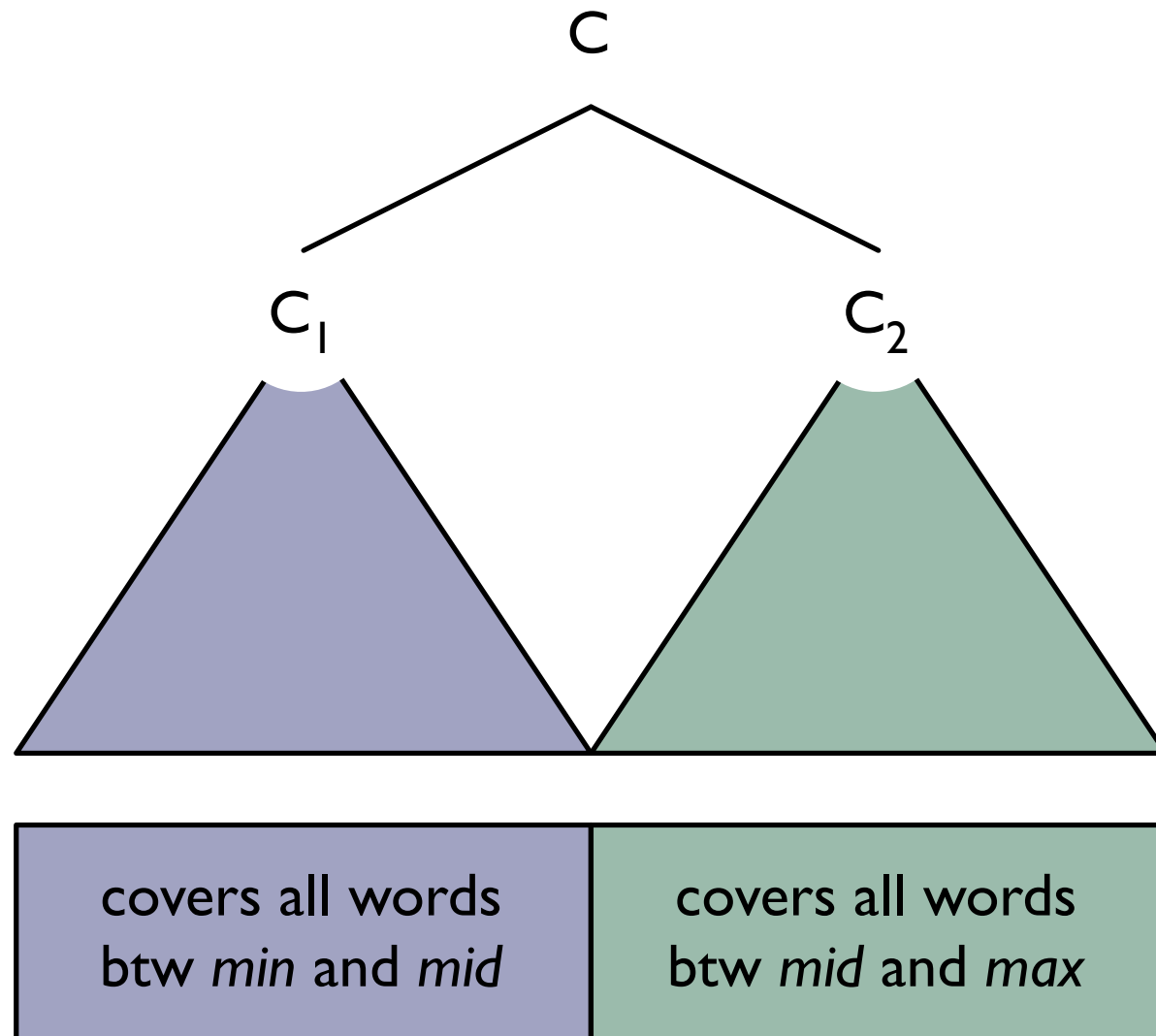
$$C \rightarrow C_1 C_2$$







# Recognizing big trees

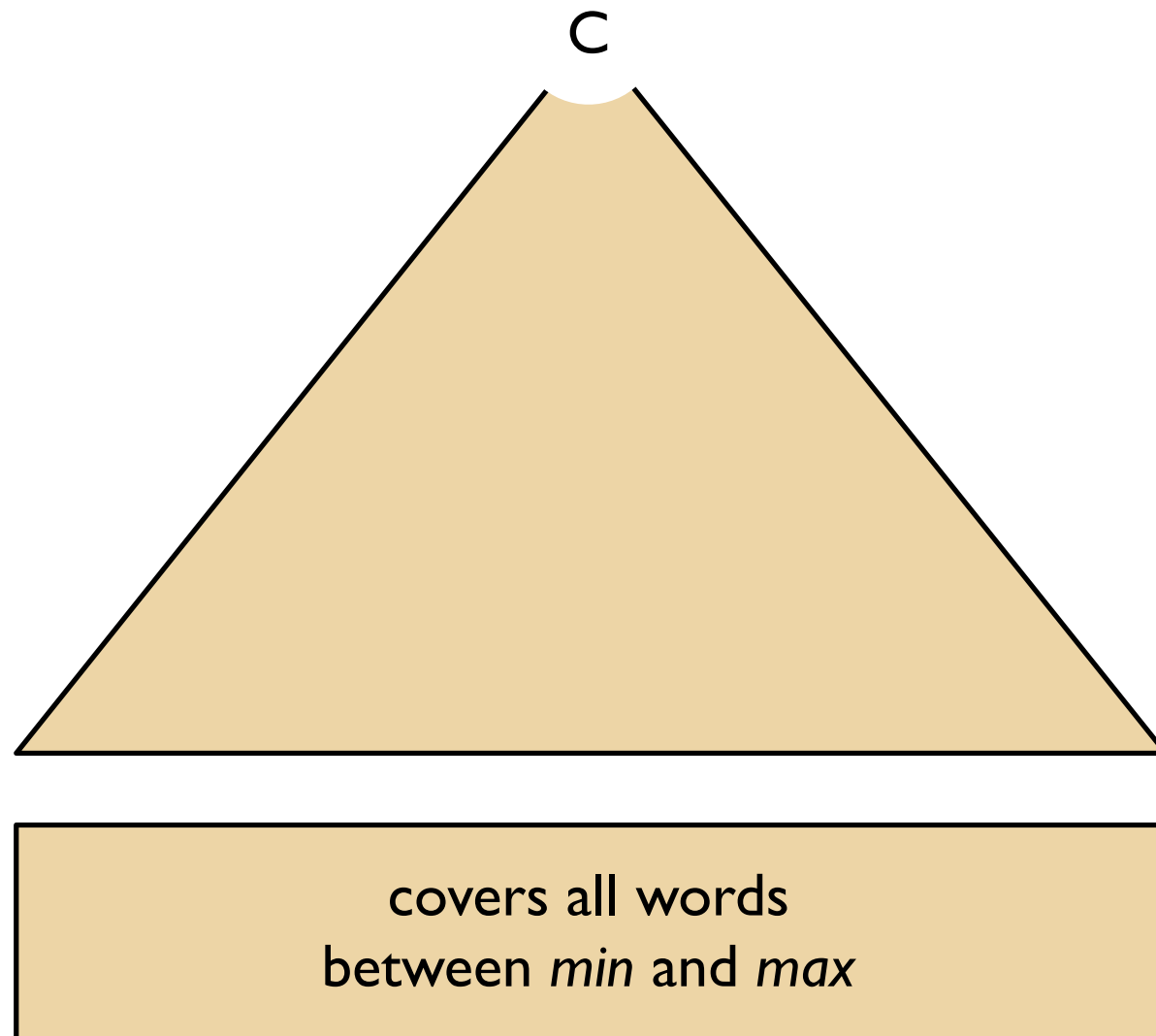




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Recognition

# Recognizing big trees





# Questions

- How do we know that we have recognized that the input sequence is grammatical?
- How do we need to extend this reasoning in the presence of unary rules:  $C \rightarrow C_1$  ?



# Signatures

- The rules that we have just seen are independent of a parse tree's inner structure.
- The only thing that is important is how the parse tree looks from the 'outside'.
- We call this the **signature** of the parse tree.
- A parse tree with **signature**  $[min, max, C]$  is one that covers all words between  $min$  and  $max$  and whose root node is labeled with  $C$ .



# Questions

- What is the signature of a parse tree for the complete sentence?
- How many different signatures are there?
- Can you relate the runtime of the parsing algorithm to the number of signatures?



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# Implementation



# Data structure

- The standard implementation represents signatures by means of a three-dimensional array *chart*.
- Initially, all entries of *chart* should be set to *false*.
- Whenever we have recognized a parse tree that spans all words between *min* and *max* and whose root node is labeled with *C*, we set the entry *chart*[*min*][*max*][*C*] to *true*.



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Implementation

# Preterminal rules

```
for each  $w_i$  from left to right
```

```
  for each preterminal rule  $C \rightarrow w_i$ 
```

```
    chart[i - 1][i][C] = true
```





# Binary rules

```
for each max from 2 to n
  for each min from max - 2 down to 0
    for each syntactic category C
      for each binary rule C -> C1 C2
        for each mid from min + 1 to max - 1
          if chart[min][mid][C1] and chart[mid][max][C2] then
            chart[min][max][C] = true
```



# Numbering of categories

- In order to use standard arrays, we need to represent syntactic categories by numbers.
- We write  $m$  for the number of categories; we number them from 0 till  $m - 1$ .
- We choose our numbers such that the start symbol  $S$  gets the number 0.



# CKY in python

- A three-dimensional array might not be the most suitable choice in python.
- It is quite possible to use more python-like data structures like dictionaries, or variants such as defaultdict
  - Use tuples as keys, e.g.  $(i, j, S)$ ; ex:  $(2, 3, \text{"Pron"})$
  - Lookup in chart: `chart[i, j, S]`
  - No need to numberize categories in this solution



# Questions

- In what way is this algorithm bottom–up?
- Why is that property of the algorithm important?
- How do we need to extend the code if we wish to handle unary rules  $C \rightarrow C_1$  ?
- Why would we want to do that?



# Summary

- The CKY algorithm is an efficient parsing algorithm for context-free grammars.
- Today: Recognizing whether there is any parse tree at all.
- Next time: Probabilistic parsing – computing the most probable parse tree.



# Reading

- Recap of the introductory lecture:  
J&M chapter 12.1-12.7 and 13.1-13.3
- CKY recognition:  
J&M section 13.4.1
- CKY probabilistic parsing, for next week:  
J&M section 14.1-14.2